



# GRAMMATICAL INFLUENCES IN A BAYESIAN SPEECH PRODUCTION FRAMEWORK

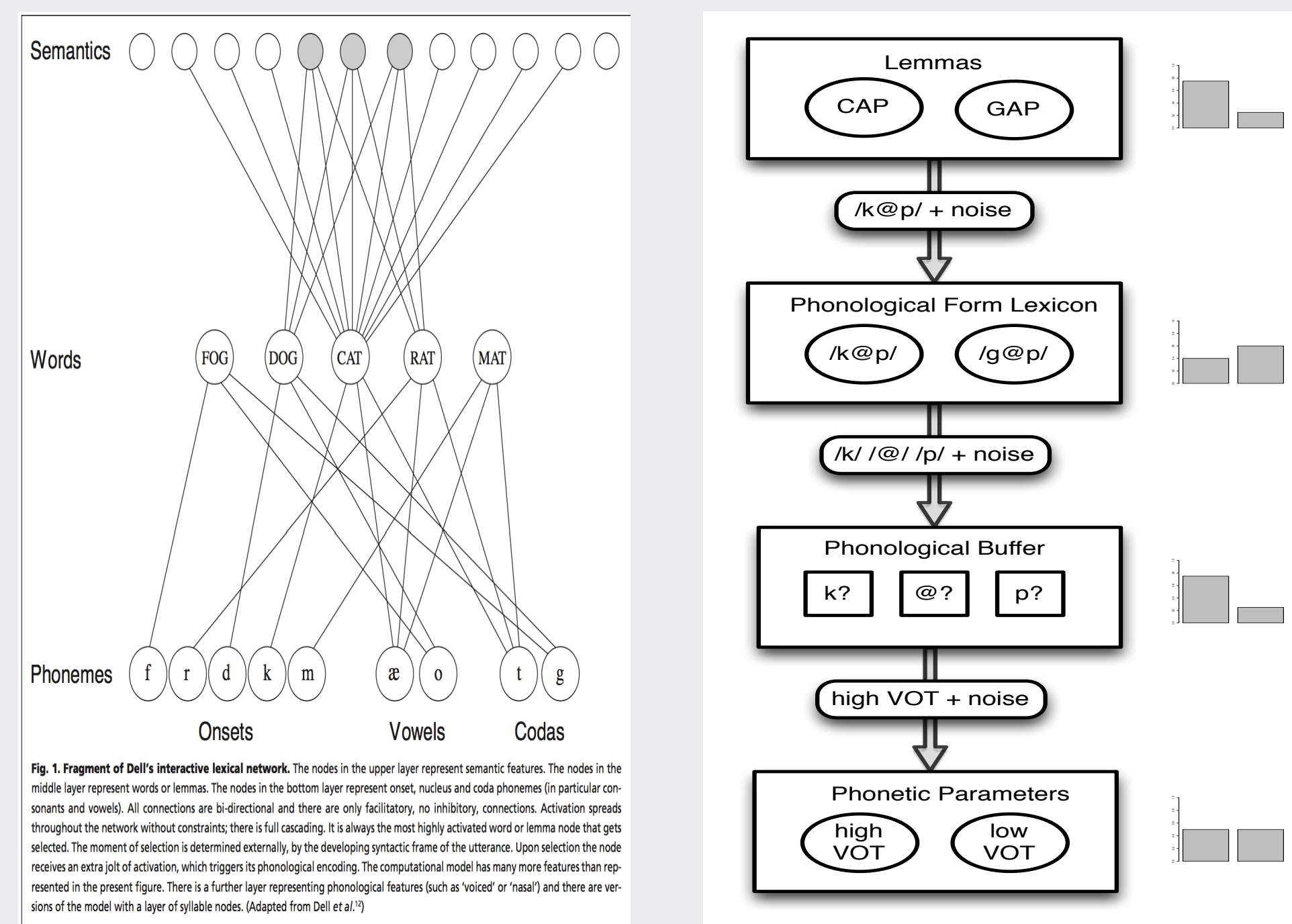


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## GRAMMATICAL INFLUENCES

- Speech planning is known to be affected by competition. Choosing between multiple similar options results in longer latencies and hyper-articulated (carefully pronounced) speech [1].
- But, language-specific knowledge and biases (grammar) *also* affect the production of both known and novel utterances.
  - Phonotactic knowledge affects the speed and accuracy of word-form repetition for both real and nonce words [2].
- Most production models do not take the latter into account.

## BAYESIAN PRODUCTION FRAMEWORK



- Most production models involve communication between multiple levels of processing.
- Bayesian model assumed here [1] treats communications as evidence to update a probability distribution over what forms to produce. Updates repeat until some form reaches threshold probability.

$$p(r|E) = \frac{p(E|r)p(r)}{Z}$$

$$\text{posterior} = \frac{\text{likelihood} * \text{prior}}{\text{normalizing constant}}$$

- **Prior** encodes which representations are possible or expected — allows inclusion of task-specific knowledge (including **grammar**), and traces of previous productions.

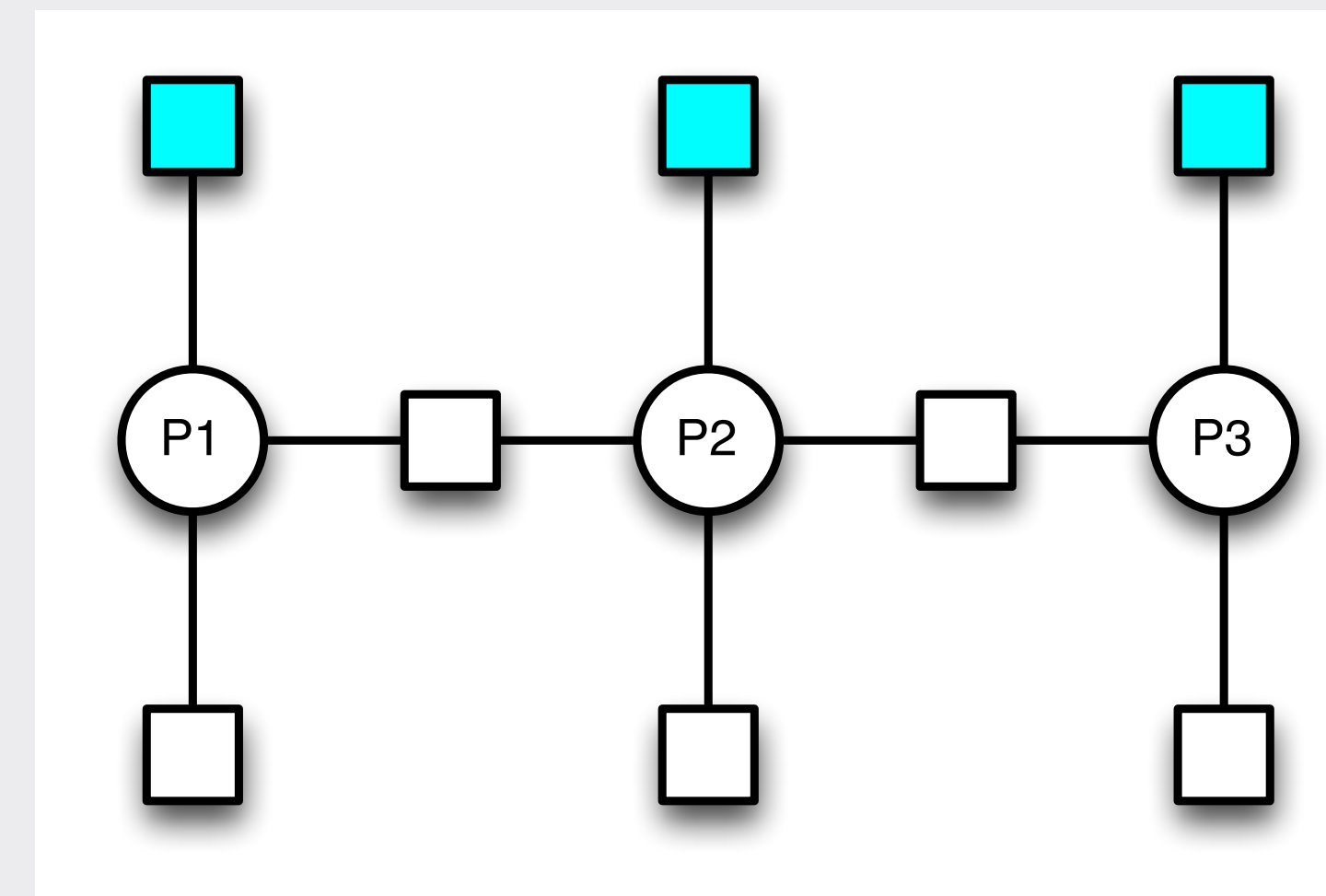
- At phonological levels, need to structure **prior** so that:
  - It can assign probabilities to arbitrary strings to allow for production of novel utterances.
  - It can incorporate grammatical knowledge.

## FACTOR GRAPHS

- Denote a string  $s$  as  $x_1x_2x_3...x_n$ , where  $x_1$  is the phone at position 1 in the string, and so on.
- $P(s)$  is a joint distribution over several random variables,  $X_1$  to  $X_n$ , one for each position in the string
- Represent distribution as a product of factors.

$$P(s) = \frac{1}{Z} \prod_i f_i(x_i(s))$$

- Graphs connect variable nodes (circles) with factor nodes (squares).
- Unitary factors represent likelihood of a certain variable value. Some (blue) can represent evidence aggregated over time.
- N-ary factors represent co-occurrence constraints.
- There are efficient inference algorithms for values of interest such as the most probable arrangement of variable states (e.g., phonemes).



## HARMONIC GRAMMARS AS GRAPHS

- Harmonic grammars are a similar formalism to Optimality Theory.
- Harmonic grammars represent the *goodness* or a form by its *harmony*.
- Harmony is calculated as the sum of weighted constraint violations, where each constraint applies e.g., to a subset of positions in a phonological string.

$$h(x_1x_2...x_n) = \sum_i w_i C_i$$

- By taking the exponent of the harmony, we get a proportional Max-Ent score [3]:

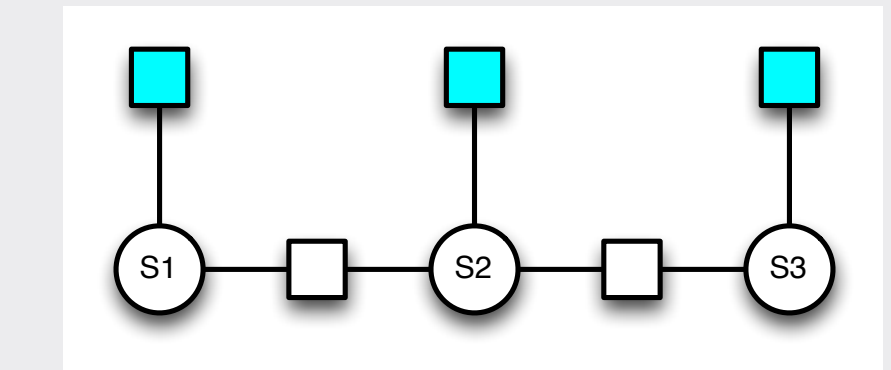
$$e^{h(x_1x_2...x_n)} = e^{\sum_i w_i C_i}$$

- Thanks to the properties of exponentiation, we can represent this as a *product* of factors, which is all we need to generate a factor graph!:

$$e^{\sum_i w_i C_i} = e^{w_1 C_1} e^{w_2 C_2} ... e^{w_N C_N} = f_1 f_2 ... f_N$$

## BERBER SYLLABIFICATION

Base harmonic grammar [4] based on Dell and Elmedlaoui [5]. Variables have two possible states, **nucleus** and **non-nucleus**:



Unitary factors (blue):

- $e^0$  for non-nucleus state
- $e^{2^s-1}$  for nucleus state, where  $s$  is the sonority of the most likely segment in position one.

Binary Factors:

- $e^0$  for when the two adjacent positions are not both nuclei
- $e^{-2^s}$  when the two adjacent positions are both nuclei

## PHONOTACTICS

- Learn phonotactic factors based on three-segment words in the Hoosier Mental Lexicon.
- CVC words greatly outnumber all other structures such CCV (1338 to 275).
- In simulations, words with optimal phonotactics (i.e., CVCs) were produced in an average of 68.5 time steps. Words with other structures were produced in an average of 76.35 time steps.

## FUTURE DIRECTIONS

- Moving beyond proof-of-concept simulations to test predictions of more detailed grammars - e.g., the full-scale phonotactic grammars induced by the Hayes/Wilson MaxEnt Learner [3].
- Thinking about plausibility as a neural mechanism:
  - Inference at each simulated time step is currently treated as instantaneous - should it have a temporal dimension? Do abstract grammatical processes such as allophonic variation have one?
  - Some neurons appear to perform probabilistic calculations, including normalization [6].

## REFERENCES

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